

COMPUTER-AIDED SEMICONDUCTOR DEVICE ANALYSES\*

by

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- (a) JUNCTION-GATE FIELD-EFFECT TRANSISTORS
- (b) ONE-DIMENSIONAL  $N^+$ -N- $N^+$  STRUCTURES

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The steady-state operation of a junction-gate field-effect transistor (JFET) with n-channel is described by the following set of equations.

$$\nabla^2 \Psi = -2\alpha[N(x,y) - n(x,y)] \quad (1)$$

$$\nabla \cdot J_n = \nabla \cdot \left[ -\frac{1}{\alpha} n(x,y) \mu_n \nabla \varphi_n \right] = 0 \quad (2)$$

$$n(x,y) = e^{\frac{\Psi - \varphi_n}{kT}} \quad (3)$$

The symbols used in equations (1) - (3) are

$\Psi$  = electro-static potential normalized by  $kT/q$

$\varphi_n$  = quasi-Fermi level for electrons normalized by  $kT/q$

$N$  = donor concentration normalized by  $N_D$

$n$  = electron concentration normalized by  $N_D$

$N_D$  = donor concentration of the n-region

$\mu_n$  = electron mobility normalized by  $\mu_{no}$

$\mu_{no}$  = low field electron mobility

$V_p$  = pinch-off voltage =  $\frac{qN_D}{2\epsilon\epsilon_0} a^2$

$2a$  = width of the n-region

$\alpha$  =  $qV_p/kT$

$J_n$  = electron current density normalized by  $q\mu_{no} N_D V_p/a$

$x, y$  = linear dimensions  $X, Y$  normalized by  $a$

Figure 1 shows the model of a JFET to be considered. The region of interest to which equations (1) - (3) are to be applied is a

plane bounded by  $X = 0$ ,  $X = L_o$ ,  $Y = a$ , and  $Y = -a$ . The variations of equations (1) - (3) suitable for machine computation are

$$\nabla^2 \Psi = -2\alpha [N(x,y) - e^{\Psi - \varphi_n}] \quad (4)$$

$$\left. \begin{aligned} \nabla^2 \delta \Psi - 2\alpha e^{\Psi - \varphi_n} \delta \Psi &= -\nabla^2 \Psi_a - 2\alpha [N(x,y) - e^{\Psi_a - \varphi_n}] \\ \Psi &= \Psi_a + \delta \Psi \end{aligned} \right\} \quad (5)$$

$$\left. \begin{aligned} \varphi_n(x) &= QN_i - \ln [e^{-\varphi_n(\ell_o) + QN_i} + \alpha I_D w(x)] \\ x &\in T_i \end{aligned} \right\} \quad (6)$$

$$I_D = \frac{1}{\alpha} [e^{-\varphi_n(o) + QN_1} - e^{-\varphi_n(\ell_o) + QN_1}] / w(o) \quad (7)$$

$$\left. \begin{aligned} w(x) &= \int_x^{\ell_o} \exp[-\Psi(t, o) + QN_i + \xi(t)] dt \\ x &\in T_i \end{aligned} \right\} \quad (8)$$

$$\xi(x) = -\ln \int_{-1}^1 \exp[\Psi(x, y) - \Psi(x, o) + \ln \mu_n] dy \quad (9)$$

where

$$\ell_o = \frac{L_o}{a}$$

$$T_1 = \{x | o \leq x \leq x_1\}$$

$$T_i = \{x | x_{i-1} < x \leq x_i\} \quad i = 2, 3, \dots, M$$

$$0 < x_1 < x_2 < \dots < x_M = \ell_o$$

$QN_i$  = reference level for  $\varphi_n$  in the subinterval  $T_i$

The field-dependent mobility for n-type silicon is approximated by

$$\mu_n = 1 - \frac{1}{2} \frac{E}{E_c} \quad E/E_c < 10^{-4}$$

$$\mu_n = \frac{1 - e^{-E/E_c}}{E/E_c} \quad E/E_c \geq 10^{-4}$$

where  $E_c = 7.77$  KV/cm.

Subroutine BOUND solves equation (4) by the generalized Newton's method along the line  $X = 0$  and  $X = L_o$ . The solutions are then used as the boundary conditions of the two-dimensional problem. Subroutine REF determines the subintervals  $T_i$  and the reference levels  $QN_i$ . The number of the subintervals is given by the input data. Subroutine FIRSTV solves equation (4) for the whole region of interest by the generalized Newton's method and subroutine COMPV solves equation (5) by successive over-relaxation method. Equations (6) - (9) are computed in subroutine COMPQ. The integration is performed by using Gaussian quadrature DQG32 in subroutine EXINT. The integrand is given by the function subprogram EFCT. The relaxation factor  $\omega$  is determined in subroutine COME at the 16th iteration.

In the main program,  $\alpha$ , doping levels, and the distribution of the donor concentration are first read from the input data. This defines the particular model to be considered. The number

of subintervals, EPS, and the first approximation of  $\varphi_n$  are given for each bias conditions. The potentials ( $\Psi$  and  $\varphi_n$ ) are normalized by  $V_p$  in input and output while they are normalized by  $kT/q$  during the computation. EPS is a small constant and used to terminate the iteration scheme. The first approximation of the electro-static potential is arbitrary but the computing time is considerably reduced with a good approximation. The main program gives this approximation by solving the one-dimensional Poisson's equation along  $y$ .

$$\frac{d^2\Psi}{dt^2} = -2\alpha N(x,t) \quad 0 \leq t \leq b$$

where

$$t = l - y$$

Using the boundary conditions

$$\frac{d\Psi}{dt}(t=b) = 0$$

$$\Psi(t=0) = \Psi(x,0)$$

we obtain

$$\Psi(x,t) = \Psi(x,0) + 2\alpha \int_0^t \eta N(x,\eta) d\eta + 2\alpha t \int_t^b N(x,\eta) d\eta \quad 0 \leq t \leq b$$

$$\Psi(x,t) = \varphi_n(x) + \ln \frac{N(x,1)}{N(x,0)} = \Psi_c \quad t > b$$

$b$  is determined by

$$\Psi_c = \Psi(x,0) + 2\alpha \int_0^1 \eta N(x,\eta) d\eta$$

If

$$\Psi_c > \Psi(x, 0) + 2\alpha \int_0^L \eta N(x, \eta) d\eta$$

$\Psi$  is given by

$$\Psi(x, t) = \Psi_c + [\Psi(x, 0) - \Psi_c] (t-1)^2$$

The program shown in the following pages is for a JFET with  $L_o = 4a$ . Depending on the input data for the donor concentration, this program can be used for both the short device ( $L/a = 2$ ) and the graded-channel device. Devices with larger values of  $L/a$  can be solved by a program similar to the one shown. Larger dimensions are necessary for these devices.

For a one-dimensional  $N^+ - N - N^+$  structure, the pertinent equations are similar to equations (4) - (9).

$$\frac{d^2\Psi}{dx^2} = -2\alpha [N(x) - e^{\Psi - \varphi_n}] \quad (10)$$

$$\left. \begin{aligned} \frac{d^2}{dx^2} (\delta\Psi) - 2\alpha e^{\Psi_a - \varphi_n} \delta\Psi &= -\frac{d^2\Psi_a}{dx^2} - 2\alpha [N(x) - e^{\Psi_a - \varphi_n}] \\ \Psi &= \Psi_a + \delta\Psi \end{aligned} \right\} \quad (11)$$

$$\varphi_n(x) = QN_i - \ln [e^{-\varphi_n(L_o) + QN_i} + \alpha JW(x)] \quad x \in T_i \quad (12)$$

$$w(x) = \int_x^{\ell_o} e^{-\Psi(t) - \ln u_n + QN_i} dt \quad x \in T_i \quad (13)$$

$$J = \frac{1}{\alpha} \frac{e^{-\varphi_n(0) + QN_1} - e^{-\varphi_n(\ell_o) + QN_1}}{w(0)} \quad (14)$$

Since the N<sup>+</sup>-N junctions are step-junctions, the distribution of the donor concentration is simple and given in the main program. Subroutines are similar to those for a JFET and are self explanatory.

JUNCTION-GATE FIELD-EFFECT  
TRANSISTORS

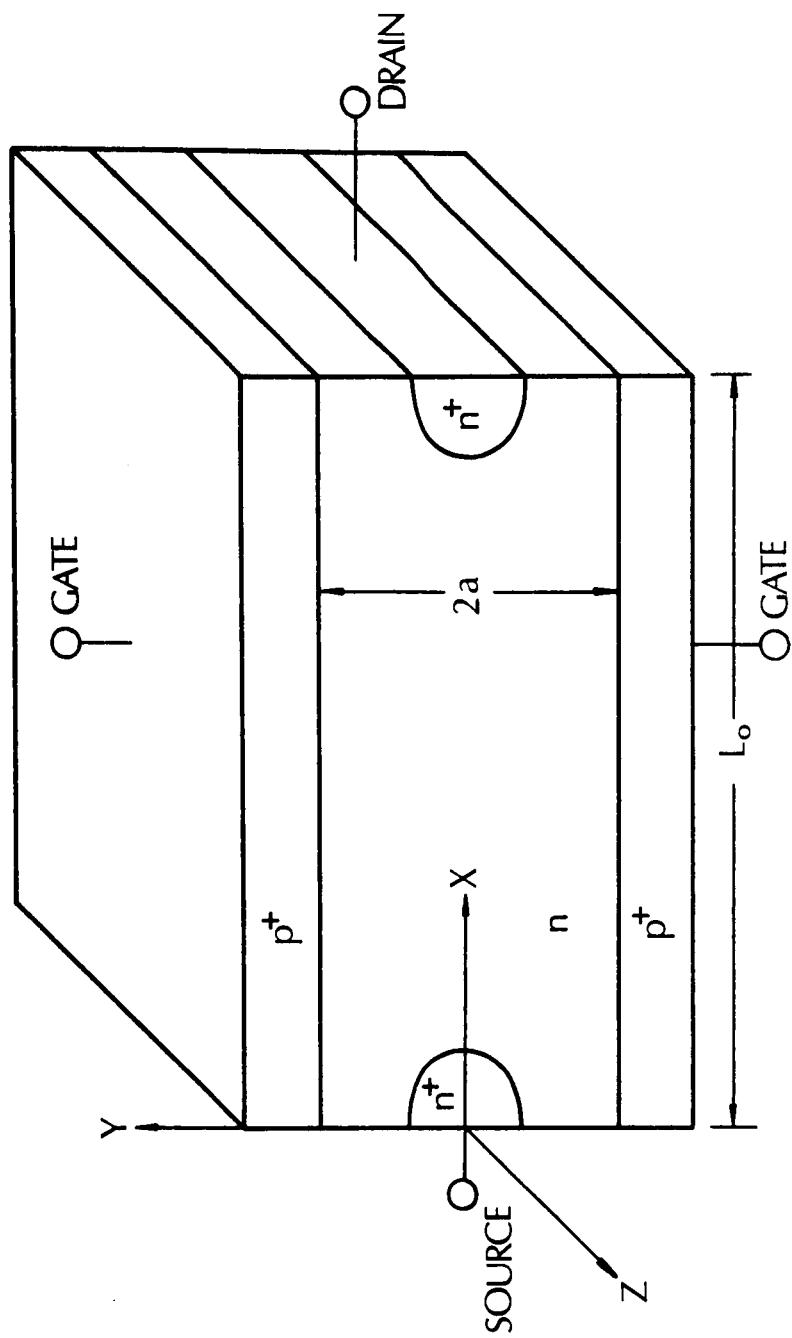


Figure 1. Device Model of Junction-Gate Field-Effect Transistors

FORTRAN IV G LEVEL 1, MOD 3

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```
0001      COMMON /BLV/V(41,81),BETA,E(41,81) /BLDDC/DDD(21,81)
          1           /BLQ/Q(81),H,EC,DC,ALP /BLRQ/QN(20),NN(20)
0002      DOUBLE PRECISION E,H,Q,V,AN,A1,A2,DC,EC,QN,ALP,BETA
C
C DIMENSION
C
0003      LX1 = 41
0004      LXC = 21
0005      LY1 = 81
0006      LYC = 41
0007      LX2 = LX1 - 1
0008      LY2 = LY1 - 1
C
C GEOMETRIC PARAMETERS AND DOPING LEVELS
C
0009      READ( 5,1 ) ALP, BND, BNA, BNI, BNDD
0010      1 FORMAT( F10.1, 1P4E10.2 )
          WRITE( 6,2 ) ALP, BND, BNA, BNI, BNDD
0011      2 FORMAT( '1', 'ALPHA = VP/VT =', F6.1 /
          1           '0', 'L/A = LENGTH TO WIDTH RATIO = 2 ' /
          2           '0', 'ND =', 1PE10.2, 1X, 'PER C.C.' /
          3           '0', 'NA =', 1PE10.2, 1X, 'PER C.C.' /
          4           '0', 'NI =', 1PE10.2, 1X, 'PER C.C.' /
          5           '0', 'ND+ =', 1PE10.2, 1X, 'PER C.C.' // )
C
0013      H = 1. / (LXC - 1.)
0014      A0 = 0.02586 * ALP
0015      A1 = DSQRT(0.24*8.8545*A0/(1.601*(BND/1.0E+15)))
0016      A2 = 7.77
0017      VB = A0*G( (BND/BNI)*(BNA/BNI) )*0.02586
0018      A = 1.0 / DSQRT(2.*ALP)
C
0019      WRITE( 6,3 ) A0, A1, VB, A2, H, A
0020      3 FORMAT( '0','VP=PINCH-CFF VOLTAGE =',F7.3,1X,'VOLTS' /
          1'0','A=HALF OF THE CHANNEL WIDTH =',F6.3,1X,'MICRON' /
          2'0','VB=BUILT IN POTENTIAL AT P-N JUNCTION =',F7.4,1X,
          3'VOLTS'/
          4'0','CRITICAL ELECTRIC FIELD =',F6.3,1X,'KV/CM'/
          5'0','MESH SIZE =',F6.3,1X,'A' /
          6'0','EXTRINSIC DEBYE LENGTH =',F6.3,1X,'A' // )
C
0021      VB = VB / 0.02586
0022      BETA = 2.*ALP*(H**2)
0023      EC = (2.*H)*(A2*0.1)*A1/0.02586
C
C DOPING PROFILE
C
0024      READ( 5,5 ) ((DDD(I,J),I=1,11),J=1,21)
```

FORTRAN IV G LEVEL 1, MCD 3

MAIN

DATE = 69329

14/56

```
0025      READ( 5,5 )  ((DCD(I,J),I=11,21),J=1,21)
0026      5 FORMAT( 11F6.3 )
0027      DO 6 I = 1, LXC
0028      DC 6 J = 22, LYC
0029      6 DCD(I,J) = 1.0
0030      DC 7 J = LYC, LY1
0031      JJ = LY1 + 1 - J
0032      DC 7 I = 1, LXC
0033      7 DCD(I,J) = DCD(I,JJ)
0034      DO 8 I = 1, LXC
0035      DO 8 J = 1, LY1
0036      8 DCD(I,J) = DCD(I,J)*BETA
0037      BETA = DLOG(BETA)

C
C BIAS CONDITIONS, NUMBER OF SUBINTERVALS, AND EPS
C
0038      10 READ( 5,11 )  VGS, VDS, NRQ, EPS
0039      11 FORMAT( 2F6.2, I6, 1P12.3 )
0040      IF( NRQ .EQ. 0 ) STCP
0041      WRITE( 6,12 )  VGS, VDS
0042      12 FORMAT( '1', 'VGS =', F5.2, 1X, '(VP-VB)' /
1           '0', 'VDS =', F5.2, 1X, '(VP-VB)' / )

C
0043      READ( 5,9 )  (Q(J),J=1,81,10)
0044      9 FORMAT( 1P7D10.3 )
0045      DO 156 J = 1, 8
0046      K = (J-1)*10
0047      DO 156 I = 2, 10
0048      156 Q(K+I) = (Q(K+10+1)-Q(K+1))*(I-1)/10. + Q(K+1)
0049      Q(LY1) = 0.0
0050      Q(1) = Q(LY1) - VDS*(ALP-VB)
0051      V(1,1) = Q(1) - VGS*(ALP-VB) - VB

C
C BOUNDARY CONDITION AT THE GATE
C
0052      DO 13 J = 1, LY1
0053      V(1,J) = V(1,1)
0054      13 V(X1,J) = V(1,J)

C
C FIRST APPROXIMATION OF THE QUASI FERMI LEVEL
C
0055      DO 14 J = 2, LY2
0056      14 Q(J) = Q(1) + ALP*Q(J)

C
C FIRST APPROXIMATION OF THE ELECTRO-STATIC POTENTIAL
C
0057      DO 23 J = 1, LY1
0058      AD = Q(J) + ALCG(DCD(LXC,J)/DCD(1,J))
```

FORTRAN IV G LEVEL 1, MOD 3

MAIN

DATE = 69329

14/56

```
0059      DO 15 I = 2, LXC
0060      V(I,J) = V(I-1,J)+((I-2)*DOD(I-1,J)+(I-1)*DOD(I,J))/2.
0061      NB = I
0062      IF( V(I,J) .GE. A0 ) GO TO 16
0063 15 CONTINUE
0064 16 IF( NB .EQ. LXC .AND. V(LXC,J) .LT. A0 ) GO TO 19
0065      DO 17 I = NB, LXC
0066 17 V(I,J) = A0
0067      A2 = 4*(A0-V(NB-1,J)) / (DOD(NB-1,J)+DCD(NB,J))
0068      A2 = DSQRT(A2 + (NB-1)**2)
0069      A2 = (DOD(NB-1,J)+DCD(NB,J))*(A2-NB+1)/2
0070      V(NB-1,J) = V(NB-1,J) + (NB-2)*A2
0071      NB = NB - 2
0072      DC 18 I = 2, NB
0073      A1 = I - 1
0074      V(I,J) = V(I,J) + A2*A1
0075      DO 18 K = I, NB
0076 18 V(I,J) = V(I,J) + A1*(DOD(K,J)+DCD(K+1,J))/2.
0077      GO TO 21
0078 19 A2 = V(I,J) - A0
0079      DO 20 I = 2, LXC
0080      A1 = H*(I-1)
0081      20 V(I,J) = A0 + A2*(A1-1.)**2
0082      21 DO 22 I = 2, LXC
0083      II = LX1 + 1 - I
0084      22 V(II,J) = V(I,J)
0085 23 CONTINUE
C
C BOUNDARY CONDITION AT THE SOURCE
C
0086      WRITE( 6,30 )
0087 30 FORMAT( //// '0', 'BOUNDARY CONDITION AT THE SOURCE'//)
0088      CALL BCUND(1,LXC)
C
C BOUNDARY CONDITION AT THE DRAIN
C
0089      WRITE( 6,31 )
0090 31 FORMAT( //// '0', 'BOUNDARY CONDITION AT THE DRAIN'//)
0091      CALL BCUND(LY1,LXC)
C
C PREPARATION OF THE ITERATION
C
0092      CALL REF(VDS,NRQ,LY1)
0093      CALL FIRSTV(LX1,LX2,LXC,LY2)
C
C ITERATION
C
0094 40 FCRMAT( '1' )
```

FORTRAN IV G LEVEL 1, MCD 3

MAIN

DATE = 69329

14/56

```
0095      K = 1
0096      41 WRITE( 6,40 )
0097      42 CALL CCMPO(LXC,LY1,LY2,NRQ)
0098      WRITE( 6,43 ) K, DC
0099      43 FORMAT( '0', 2X, 'K =', I3, 3X, 'DRAIN CURRENT =',
1          1PD11.4 )
0100      CALL COMPV(LX1,LX2,LXC,LY1,LY2,RMAX)
0101      IF( RMAX .LT. EPS ) GO TO 50
0102      IF( K .GE. 50 ) GO TO 50
0103      K = K + 1
0104      IF( K.EQ. 19.OR.K.EQ. 37 ) GO TO 41
0105      GO TO 42
C
C COMPUTE FOR THE CUTPUT
C
0106      50 DO 53 I = 1, LXC
0107          DO 53 J = 1, LY1
0108          53 E(I,J) = DEXP(V(I,J)-Q(J))
C
0109          A0 = Q(1)
0110          DO 54 J = 1, LY1
0111          54 Q(J) = (C(J)-A0) / ALP
C
0112          A0 = V(1,1)
0113          DO 55 J = 1, LY1
0114              DO 55 I = 1, LXC
0115              55 V(I,J) = (V(I,J)-A0) / ALP
C
C CUTPUT
C
0116      WRITE( 6,61 )
0117      61 FORMAT( '1', 'ELECTRC-STATIC POTENTIAL', 5X, 'PAGE 1' / )
0118          WRITE( 6,66 ) ((V(I,J),I=1,21),J,J=1,41)
0119          WRITE( 6,62 )
0120      62 FORMAT( '1', 'ELECTRC-STATIC POTENTIAL', 5X, 'PAGE 2' / )
0121          WRITE( 6,66 ) ((V(I,J),I=1,21),J,J=41,81)
C
0122          WRITE( 6,63 )
0123      63 FORMAT( '1', 'ELECTRCN DENSITY', 5X, 'PAGE 1' / )
0124          WRITE( 6,66 ) ((E(I,J),I=1,21),J,J=1,41)
0125          WRITE( 6,64 )
0126      64 FORMAT( '1', 'ELECTRON DENSITY', 5X, 'PAGE 2' / )
0127          WRITE( 6,66 ) ((E(I,J),I=1,21),J,J=41,81)
0128      66 FORMAT( ' ', 21F6.3,I3 )
C
0129          WRITE( 6,65 ) (K,K=1,10)
0130      65 FORMAT( '1', 'QUASI FERMI LEVEL' / '0', 1X, 10I12 / )
0131      67 FORMAT( '0', I4, 1X, 1P1CD12.3 )
```

FORTRAN IV G LEVEL 1, MCD 3

MAIN

DATE = 69329

14/56

```
0132      DO 68 K = 1, 8
0133      I = 10*(K-1)
0134      68 WRITE( 6,67 ) I, (Q(I+J),J=1,10)
0135      I = 80
0136      WRITE( 6,67 ) I, Q(I+1)
0137      GO TO 10
0138      END
```

**FORTRAN IV G LEVEL 1, MCD 3**

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**14/56**

**TOTAL MEMORY REQUIREMENTS 00174A BYTES**

FORTRAN IV G LEVEL 1, MOD 3

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14/56

```
0001      SUBROUTINE    REF(VDS,N,LY1)
C
0002      COMMON /BLQ/C(81) /BLRQ/CN(20),NN(20)
0003      DOUBLE PRECISION Q,CN,A0,A1,A2
C
0004      IF( VDS .EQ. 0.0 ) RETURN
0005      NN(1) = 1
0006      M = N - 1
0007      A1 = (C(LY1)-C(1))/M
0008      A0 = A1 / 2.
0009      CN(1) = C(1) + A0
0010      DO 2 I = 2, M
0011      CN(I) = CN(I-1) + A1
0012      NN(I) = NN(I-1) + 1
0013      K = NN(I) + 1
0014      A2 = CN(I-1) + A0
0015      DO 1 J = K, LY1
0016      IF( Q(J) .LE. A2 ) NN(I) = J
0017      IF( Q(J) .GT. A2 ) GO TO 2
0018      1 CONTINUE
0019      2 CONTINUE
0020      NN(N) = LY1
C
0021      WRITE( 6,21 ) (K,K=1,10)
0022      21 FORMAT( '1', 'FIRST APPROXIMATION OF THE QUASI FERMI
1          LEVEL' / '0', 1X, 10I12 / )
0023      DO 22 I = 1, 8
0024      K = 10*(I-1)
0025      22 WRITE( 6,23 ) K, (C(K+J),J=1,10)
0026      23 FORMAT( '0', 14, 1X, 1P10D12.3 )
0027      K = 80
0028      WRITE( 6,23 ) K, Q(K+1)
0029      WRITE( 6,24 )
0030      24 FORMAT( // '0', 9X, 'J', 7X, 'NN(J)', 6X, 'QN(J)' // )
0031      DO 25 I = 1, N
0032      25 WRITE( 6,26 ) I, NN(I), CN(I)
0033      26 FORMAT( ' ', 2I10, 1PE15.3 )
0034      WRITE( 6,26 ) N, NN(N)
0035      RETURN
0036      END
```

FORTRAN IV G LEVEL 1, MCD 3

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14/56

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FORTRAN IV G LEVEL 1, MCD 3

FIRSTV

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14/56

```
0001      SUBROUTINE FIRSTV(LX1,LX2,LXC,LY2)
C
0002      COMMON /BLV/V(41,81),BETA /BLQ/Q(81) /BLDCD/DOD(21,81)
0003      DOUBLE PRECISION V,BETA,Q,A0,A1,A2,ER1
C
0004      KV = 1
0005      OME = 1.0
0006      1 A2 = 0.0
0007      EER = 0.0
0008      DO 3 I = 2, LX2
0009      IF( I .LE. LXC ) II = I
0010      IF( I .GT. LXC ) II = LX1 + 1 - I
0011      DO 3 J = 2, LY2
0012      A0 = V(I+1,J)+V(I-1,J)+V(I,J+1)+V(I,J-1)
0013      A1 = DEXP(V(I,J)-Q(J)+BETA)
0014      A0 = (A0-4.*V(I,J)) + (DOD(II,J)-A1)
0015      A1 = A1 + 4.
0016      A0 = CME*(A0/A1)
0017      V(I,J) = V(I,J) + A0
0018      B = DABS(A0)
0019      IF( B .GT. EER ) EER = B
0020      3 A2 = A2 + A0**2
C
0021      IF( EER .LT. 0.005 ) GO TO 4
0022      IF( KV .GE. 200 ) GO TO 4
0023      CALL CCME(KV,A2,ER1,OME)
0024      KV = KV + 1
0025      GO TO 1
C
0026      4 WRITE( 6,5 ) KV, OME, EER
0027      5 FORMAT( //,'C','KV =',I3,3X,'OME =',F5.2,3X,'EER =',
0028                  1PE10.2 )
0029      RETURN
      END
```

FORTRAN IV G LEVEL 1, MOD 3

FIRSTV

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14/56

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FORTRAN IV G LEVEL 1, MOD 3

COMPQ

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14/56

```
0001      SUBROUTINE  COMPQ(LXC,LY1,LY2,N)
C
0002      COMMON /BLV/V(41,81) /BLQ/Q(81),H,EC,DC,ALP
1          /BLRQ/QN(20),NN(20)
0003      DOUBLE PRECISION V,Q,H,EC,DC,ALP,QN,X(81),Y(81),
1          XX(81),AO,A1,A2
C
0004      M = N - 1
0005      IF( Q(1) .EQ. Q(LY1) ) GO TO 100
0006      DO 3 J = 1, LY1
0007      DO 1 I = 1, LXC
0008      K = LXC + 1 - I
0009      IF( J .EQ. 1 ) AO = 4.*V(I,J+1)-3.*V(I,J)-V(I,J+2)
0010      IF( J .EQ. LY1 ) AO = 3.*V(I,J)+V(I,J-2)-4.*V(I,J-1)
0011      IF( J .GT. 1 .AND. J .LT. LY1 ) AO = V(I,J+1)-V(I,J-1)
0012      A1 = DABS(AO/EC)
0013      IF( A1 .LT. 1.0D-4 ) A2 = 1. - A1/2.
0014      IF( A1 .GE. 1.0D-4 ) A2 = (1.-DEXP(-A1))/A1
0015      A2 = DLCG(A2)
0016      1 XX(K) = V(I,J) - V(LXC,J) + A2
0017      CALL EXINT(H,1,LXC,XX,Y,O,O,LXC)
0018      3 X(J) = -DLCG(Y(1))
C
0019      Y(LY1) = 0.0
0020      DC 7 I = 1, M
0021      K = N - I
0022      JS = NN(K)
0023      JL = NN(K+1)
0024      DC 5 J = JS, JL
0025      5 XX(J) = -V(LXC,J) + X(J) + QN(K)
0026      CALL EXINT(H,JS,JL,XX,Y,Y(JL),LY1)
0027      IF( K .EC. 1 ) GO TO 7
0028      IF( Y(JS) .EQ. 0.0 ) AO = -1000.
0029      IF( Y(JS) .NE. 0.0 ) AO = DLOG(Y(JS))
0030      Y(JS) = DEXP(QN(K-1)-QN(K)+AO)
0031      7 CONTINUE
C
0032      DC 9 J = 1, LY2
0033      AO = Y(J)
0034      IF( AO .EQ. 0.0 ) Y(J) = -1000.
0035      IF( AO .NE. 0.0 ) Y(J) = DLOG(Y(J))
0036      9 CONTINUE
C
0037      AO = -Q(LY1) + QN(1) - Y(1)
0038      A1 = -Q(1) + QN(1) - Y(1)
0039      DC 11 J = 2, LY2
0040      DO 10 I = 1, M
0041      IF( J .GT. NN(I) .AND. J .LE. NN(I+1) ) K = I
```

FORTRAN IV G LEVEL 1, MOD 3

CUMPQ

DATE = 69329

14/56

```
0042      10 CONTINUE
0043      Q(J) = DEXP(QN(K)-Q(LY1))
0044      Q(J) = Q(J) - DEXP(A0 + Y(J))
0045      Q(J) = Q(J) + DEXP(A1 + Y(J))
0046      11 Q(J) = QN(K) - DLOG(Q(J))
C
0047      DC = DEXP(QN(1)-Q(1)-Y(1)) - DEXP(QN(1)-Q(LY1)-Y(1))
0048      DC = 2.*DC/ALP
0049      RETURN
0050 100 DC = 0.0
0051      RETURN
0052      END
```

FCRTRAN IV G LEVEL 1, MOD 3

COMPQ

DATE = 69329

14/56

TOTAL MEMORY REQUIREMENTS 001052 BYTES

FORTRAN IV G LEVEL 1, MCD 3

COMPV

DATE = 69329

14/56

```
0001      SUBROUTINE COMPV(LX1,LX2,LXC,LY1,LY2,RMAX)
C
0002      CCMCN /BLV/V(41,81),BETA,E(41,81) /BLQ/Q(81)
U      /BLDCD/DOD(21,81)
0003      DOUBLE PRECISION D(41,81),R(40,80),E,Q,V,A0,A1,A2,
1          ERI,BETA
C
0004      RMAX = 0.0
0005      DO 2 I = 2, LX2
0006      IF( I .LE. LXC ) II = I
0007      IF( I .GT. LXC ) II = LX1 + 1 - I
0008      DO 2 J = 2, LY2
0009      A0 = V(I+1,J)+V(I-1,J)+V(I,J+1)+V(I,J-1)-4.*V(I,J)
0010      E(I,J) = DEXP(V(I,J)-Q(J)+BETA)
0011      R(I,J) = A0 + (DOD(II,J) - E(I,J))
0012      B = DABS(R(I,J))/DOC(II,J)
0013      IF( B .GT. RMAX ) RMAX = B
0014      2 CONTINUE
0015      DO 3 I = 1, LX1
0016      DO 3 J = 1, LY1
0017      3 D(I,J) = 0.0
C
0018      KD = 1
0019      CME = 1.0
0020      10 DMAX = 0.0
0021      A2 = 0.0
0022      EER = 0.0
0023      DO 4 I = 2, LX2
0024      DO 4 J = 2, LY2
0025      A0 = D(I+1,J) + D(I-1,J) + D(I,J+1) + D(I,J-1)
0026      A1 = 4. + E(I,J)
0027      A0 = UME*(A0-(A1*D(I,J)-R(I,J)))/A1
0028      D(I,J) = D(I,J) + A0
0029      B = DABS(A0)
0030      IF( B .GT. EER ) EER = B
0031      B = DABS(D(I,J))
0032      IF( B .GT. DMAX ) DMAX = B
0033      4 A2 = A2 + A0**2
C
0034      IF( EER/DMAX .LT. 1.0E-02 ) GO TO 20
0035      IF( KD .GE. 100 ) GO TO 20
0036      CALL CCMC(KD,A2,ERI,OME)
0037      KD = KD + 1
0038      GO TO 10
C
0039      20 WRITE( 6,100 ) KD, OME, EER, DMAX, RMAX
0040      100 FORMAT( ' ',2X,'KD =',I3,3X,'OME =',F5.2,3X,'EER =',
1          1PE10.2,3X,'DMAX =',1PE10.2,3X,'RMAX =',1PE10.2 )
```

FORTRAN IV G LEVEL 1, MCD 3

COMPV

DATE = 69329

14/56

```
0041      DC 5   I = 2, LX2
0042      DO 5   J = 2, LY2
0043      5 V(I,J) = V(I,J) + D(I,J)
0044      RETLBN
0045      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**COMPV**

**DATE = 69329**

**14/56**

**TOTAL MEMORY REQUIREMENTS 00D33C BYTES**

FORTRAN IV G LEVEL 1, MCD 3

BOUND

DATE = 69329

14/56

```
0001      SUBROUTINE BOUND(J,NDIM)
C
0002      COMMON /BLV/V(41,81),BETA /BLQ/Q(81) /BLDD/DOD(21,81)
0003      DOUBLE PRECISION AC,A1,A2,V,Q,BETA,ER1
C
0004      MDIM = NDIM - 1
0005      CME = 1.0
0006      K = 1
0007      1 A2 = 0.0
0008      EER = 0.0
0009      DO 2 I = 2, MDIM
0010      A0 = V(I+1,J)+V(I-1,J)-2.*V(I,J)
0011      A1 = DEXP(V(I,J)-Q(J)+BETA)
0012      A0 = A0 + (DOD(I,J) - A1)
0013      A1 = 2. + A1
0014      A0 = CME*(A0/A1)
0015      V(I,J) = V(I,J) + A0
0016      B = DABS(A0)
0017      IF( B .GT. EER ) EER = B
0018      2 A2 = A2 + A0**2
C
0019      IF( EER .LT. 1.0E-04 .OR. K .GE. 150 ) GO TO 5
0020      CALL CUME(K,A2,ER1,CME)
0021      K = K + 1
0022      GO TO 1
C
0023      5 WRITE( 6,20 ) K, CME, EER
0024      20 FORMAT( ' ', 'KV =',I3,5X,'CME =',F5.2,5X,'EER =',
           1          1PE10.2 // )
C
0025      WRITE( 6,21 ) ((V(7*(K-1)+I,J),I=1,7),K=1,3)
0026      21 FORMAT( ' ', 1P7E15.3 )
0027      DC 30 I = 2, MDIM
0028      1I = MDIM*2 + 2 - I
0029      30 V(II,J) = V(I,J)
      RETURN
      END
```

FORTRAN IV G LEVEL 1, MCD 3

BOUND

DATE = 69329

14/56,

TOTAL MEMORY REQUIREMENTS 000540 BYTES

FORTRAN IV G LEVEL 1, MOD 3

EXINT

DATE = 69329

14/56

```
0001      SUBROUTINE EXINT(H,IS,IF,X,Y,Y0,NDIM)
C
C THIS SUBROUTINE INTEGRATES EXP(X) FROM IS, WHICH IS BETWEEN
C IS AND IF, TO IF AND STCRES (RESULT+Y0) AT Y(IF). H IS THE
C MESH SIZE AND NDIM IS THE MAXIMUM DIMENSION OF X AND Y.
C
0002      DOUBLE PRECISION A,H,X,Y,A0,A1,A2,Y0,H2I,HSQ2I,EFCT
0003      DIMENSION X(NDIM), Y(NDIM)
0004      COMMON /BLINT/A1,A2
0005      EXTERNAL EFCT
C
0006      H2I = 1.0 / (2.*H)
0007      HSQ2I = 1.0 / (2.*H**2)
0008      Y(IF) = Y0
0009      LAST = IF - IS
0010      DO 1  II = 2, LAST
0011      I = IF + 1 - II
0012      A0 = X(I)
0013      A1 = (X(I+1)-X(I-1))*H2I
0014      A2 = (X(I+1)+X(I-1)-2.*X(I))*HSQ2I
0015      CALL DQG32(0.0,H,EFCT,A)
0016      1 Y(I) = Y(I+1) + DEXP(A0+DLOG(A))
0017      CALL DQG32(-H,0.0,EFCT,A)
0018      Y(IS) = Y(IS+1) + DEXP(A0+DLOG(A))
0019      RETURN
0020      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**EXINT**

**DATE = 69329**

**14/56**

**TOTAL MEMORY REQUIREMENTS 00C3A8 BYTES**

FORTRAN IV G LEVEL 1, MCD 3

EFCT

DATE = 69329

14/56

```
0001      FUNCTION EFCT(Z)
C
0002      DOUBLE PRECISION A1,A2,Z,EFCT
0003      COMMON /BLINT/A1,A2
0004      EFCT = DEXP(A1*Z + A2*Z**2)
0005      RETURN
0006      END
```

FORTRAN IV G LEVEL 1, MCD 3

EFCT

DATE = 69329

14/56

TOTAL MEMORY REQUIREMENTS OCC166 BYTES

FORTRAN IV G LEVEL 1, MCD 3

COME

DATE = 69329

14/56

```
0001      SUBROUTINE  COME(KDV,ER,ERP,CME)
0002      C
0002      DOUBLE PRECISION A,ERP,ER
0003      C
0003      IF( KDV .GT. 16 ) GO TO 2
0004      A = DSQRT(ER)
0005      IF( KDV .LE. 15 ) GO TO 1
0006      AA = A/ERP
0007      BB = (AA+OME-1.)/(OME*SQRT(AA))
0008      OME = 2./(1.+SQRT(1.-BB**2))
0009      1 ERP = A
0010      2 RETURN
0011      END
```

FORTRAN IV G LEVEL 1, MOD 3

COME

DATE = 69329

14/56

TOTAL MEMORY REQUIREMENTS 00024C BYTES

ONE-DIMENSIONAL  $N^+ - N - N^+$  STRUCTURES

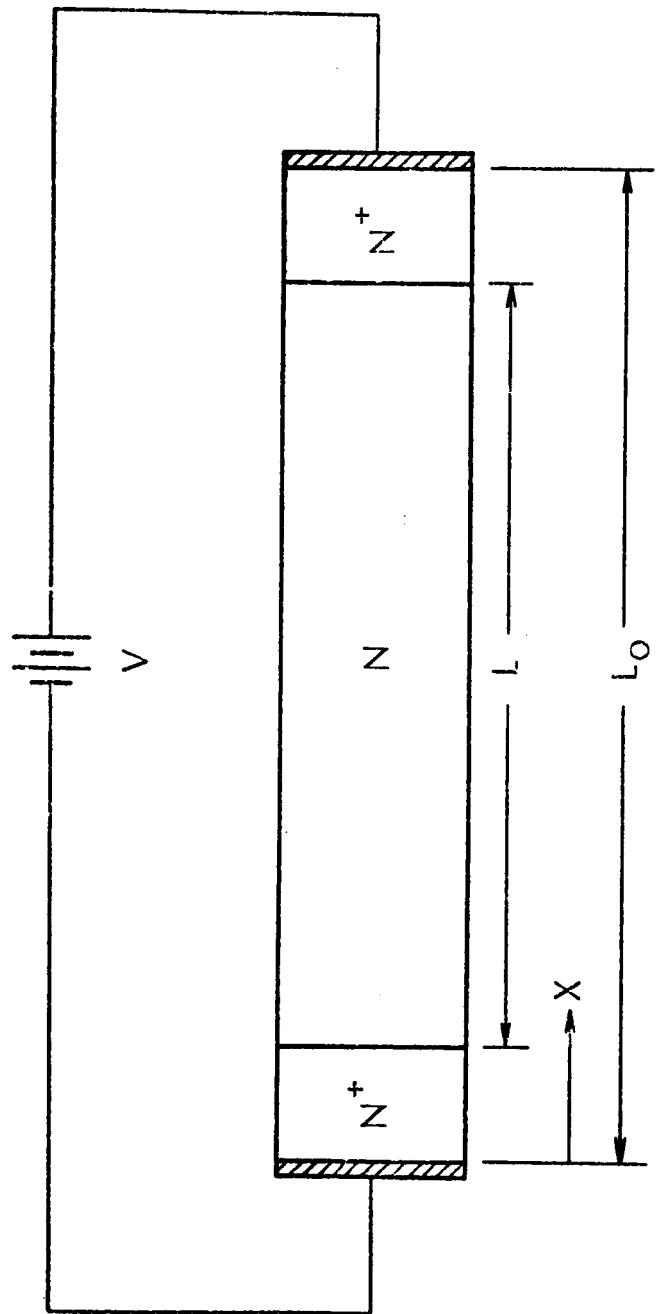


Figure 2. One-Dimensional  $N^+$ - $N$ - $N^+$  Structure

FORTRAN IV G LEVEL 1, MOD 3

MAIN

DATE = 69338

21/51/18

```
0001      COMMON /BLV/V(341),HR,BETAS,BETAL,BETASL,BETALL
1          /BLE/E(341) /BLQ/Q(341),HS,HL,EN,ALP,DC
2          /BLRQ/QN(20),NN(20) /BLDD/DOD(341)
3          /BLAUX/X(341),XX(341),Y(341)
0002      DOUBLE PRECISION V,HR,BETAS,BETAL,BETASL,BETALL,Q,HS,
1                  HL,EN,ALP,DC,QN,E,A0,A1,A2,A3,A4,DR,
2                  VB,BND,BNDD,DOD,VCE,X,Y,XX
C
0003      LXE = 41
0004      LXC = 291
0005      LXT = 331
0006      LXM = 1 + (LXT-1) / 2
0007      LXE1 = LXE - 1
0008      LXE2 = LXE + 1
0009      LXC1 = LXC - 1
0010      LXC2 = LXC + 1
0011      LXT1 = LXT - 1
C
0012      READ( 5,1 ) ALP, BND, BNDD
0013      1 FORMAT( 1PD10.1, 1P2D10.1 )
0014      DR = BNDD/BND
0015      DO 2 I = 1, LXE1
0016      DOD(I) = DR
0017      II = LXT + 1 - I
0018      2 DOD(II) = DR
0019      DO 3 I = LXE, LXC
0020      3 DOD(I) = 1.0
0021      DOD(LXE1) = 1. + (DR-1.) / 2.
0022      DOD(LXC2) = DOD(LXE1)
0023      WRITE( 6,4 ) (DOD(I),I=1,LXT)
0024      4 FORMAT( '0', 1P10D11.3 )
0025      WRITE( 6,5 ) ALP, BND, BNDD
0026      5 FORMAT( '1', 'ALPHA =', F6.1 /
1          '0', 'ND =', 1PE8.1, 1X, 'PER C.C.' /
2          '0', 'ND+ =', 1PE8.1, 1X, 'PER C.C.' // )
0027      HL = 1.0D 00 / (LXC-LXE)
0028      HR = 25.0 / DSQRT(DR)
0029      HS = HL * HR
0030      A0 = 0.02586 * ALP
0031      A1 = DSQRT(0.24*8.854*A0/(1.601*(BND/1.0E+15)))
0032      A2 = A1*(LXE-1.)*HR/(LXC-LXE)
0033      A3 = DSQRT(2.*ALP) * HL
0034      A4 = DSQRT(2.*ALP*DR) * HS
0035      VB = 0.02586*DLOG(DR)
0036      EN = 0.2586 / A1
0037      WRITE( 6,6 ) A0,A1,A2,A3,A4,HR,VB
0038      6 FORMAT('0','VO = CROSSOVER VOLTAGE =',F7.3,' VOLTS' /
1          '0','SIZE OF THE N REGION =',F6.3,' MICRONS' /
```

FORTRAN IV G LEVEL 1, MOD 3

MAIN

DATE = 69338

21/51/18.

```
2      '0','SIZE OF THE N+ REGION =',F6.3,' MICRONS' /
3      '0','(MESH SIZE/DEBYE LENGTH) IN N- REGION =',
4      F7.4 /
5      '0','(MESH SIZE/DEBYE LENGTH) IN N+ REGION =',
6      F6.3 /
7      '0','RATIO OF TWO MESH SIZES =', F6.3 /
8      '0','BUILT-IN POTENTIAL AT THE N-N+ JUNCTION ='
9      ,F6.3,' VOLTS' // )
```

C

```
0039   VB = DLOG(DR)
0040   BETAL = 2.*ALP*(HL**2)
0041   BETAS = 2.*ALP*(HS**2)
0042   DO 7 I = 1, LXE1
0043   II = LXT + 1 - I
0044   DOD(I) = DOD(I)*BETAS
0045   7 DOD(II) = DOD(I)
0046   DO 8 I = LXE, LXC
0047   8 DOD(I) = DOD(I) * BETAL
0048   BETASL = DLOG(BETAS)
0049   BETALL = DLOG(BETAL)
```

C

C READ AND WRITE THE BIAS CONDITION

```
0050 10 READ( 5,11 ) VCE, NRQ, EPS
0051 11 FORMAT( 1PD10.2, I10, 1PE10.2 )
0052   IF( NRQ .EQ. 0 ) STOP
0053   WRITE( 6,12 ) VCE
0054 12 FORMAT( '1', 'VCE =', F5.2, 1X, 'V0' // )
```

C

```
0055 Q(1) = 0.0
0056 Q(LXT) = VCE*ALP
0057 V(1) = Q(1) + VB
0058 V(LXT) = Q(LXT) + VB
```

C

C INITIAL DISTRIBUTION OF Q AND V

```
0059 13 DO 13 I = 2, LXF
0060   Q(I) = Q(1)
0061   13 V(I) = V(1)
0062   A0 = LXC - LXE
0063   IF( VCE .LT. 1.0 ) A2 = 1.0
0064   IF( VCE .GE. 1.0 ) A2 = 1.5
0065   A0 = (Q(LXT)-Q(1))/(A0**A2)
0066   DO 14 I = LXE2, LXC1
0067   A1 = I - LXE
0068   Q(I) = Q(1) + A2*A1**A2
0069   14 V(I) = Q(I)
0070   DO 15 I = LXC, LXT1
0071   Q(I) = Q(LXT)
0072   15 V(I) = V(LXT)
```

FORTRAN IV S LEVEL 1, MOD 3

MAIN

DATE = 69338

21/51/18

```
0073      CALL    REF(VCE,NRQ,LXE,LXC,LXT)
C
C ITERATION
0074      KV1 = 10
0075      K = 1
0076      21 WRITE( 6,22 )
0077      22 FORMAT( '1' )
0078      23 CALL    COMPQ(LXT,LXE,LXC,LXT1,NRQ)
0079      WRITE( 6,24 ) K, DC
0080      24 FORMAT( '0',2X,'K =',I3,3X,'CURRENT =',1PD11.4 )
0081      CALL    FIRSTV(LXT1,LXE,LXC,KV1)
0082      IF( KV1 .LT. 10 .AND. KV .LT. 10 ) GO TO 25
0083      IF( K .GE. 15 ) GO TO 25
0084      KV1 = KV
0085      K = K + 1
0086      IF( K .EQ. 19 .OR. K .EQ. 37 ) GO TO 21
0087      GO TO 23
C
0088      25 K = 1
0089      26 WRITE( 6,22 )
0090      27 CALL    COMPQ(LXT,LXE,LXC,LXT1,NRQ)
0091      WRITE( 6,24 ) K, DC
0092      CALL    COMPV(LXT,LXT1,LXE,LXC,RMAX)
0093      IF( RMAX .LT. FPS ) GO TO 30
0094      IF( K .GE. 200 ) GO TO 30
0095      K = K + 1
0096      IF( K.EQ.19.OR.K.EQ.37.OR.K.EQ.55.OR.K.EQ.73.OR.K.EQ.
1      91.OR.K.EQ.109.OR.K.EQ.127.OR.K.EQ.145.OR.K.EQ.163
3      .OR.K.EQ.181) GO TO 26
0097      GO TO 27
C
C OUTPUT
0098      30 A0 = V(1) - VB
0099      A1 = Q(1)
0100      DO 31 I = 1, LXT
0101      XX(I) = DEXP(V(I)-Q(I))
0102      V(I) = (V(I)-A0)/ALP
0103      31 Q(I) = (Q(I)-A1)/ALP
0104      WRITE( 6,32 )
0105      32 FORMAT( '1',6X,'ELECTRO-STATIC',9X,'QUASI-FERMI',12X,
1          'ELECTRON',12X,'ELECTRIC',// ',11X,'POTENTIAL',
2          11X,'POTENTIAL',13X,'DENSITY',15X,'FIELD' /
3          '0',18X,'V0',18X,'V0',18X,'ND',15X,'KV/CM'// )
0106      DO 33 I = 1, LXF
0107      33 WRITE( 6,34 ) I,V(I),Q(I),XX(I),E(I)
0108      34 FORMAT( ' ', I3, F17.5, 3F20.5 )
0109      WRITE( 6,32 )
0110      DO 35 I = LXF, LXC
```

FORTRAN IV G LEVEL 1, MOD 3

MAIN

DATE = 69338

21/51/18

```
0111      35 WRITE( 6,34 ) I,V(I),Q(I),XX(I),E(I)
0112      WRITE( 6,32 )
0113      DO 36 I = LXC, LXT
0114      36 WRITE( 6,34 ) I,V(I),Q(I),XX(I),E(I)
0115      GO TO 10
0116      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**MAIN**

**DATE = 69338**

**21/51/18**

**TOTAL MEMORY REQUIREMENTS 0011DE BYTES**

FORTRAN IV G LEVEL 1, MOD 3

REF

DATE = 69338

21/51/18

```
0001      SUBROUTINE  REF(VCE,N,LXE,LXC,LXT)
0002      C
0003      COMMON /BLQ/Q(341) /BLRQ/QN(20), NN(20)
0004      DOUBLE PRECISION Q,QN,A0,A1,A2
0005      C
0006      WRITE( 6,20 )
0007      20 FORMAT( '0', // )
0008      IF( VCE .EQ. 0.0 ) RETURN
0009      NN(1) = 1
0010      NN(2) = LXE
0011      QN(1) = Q(1)
0012      M = N - 2
0013      A1 = (Q(LXT)-Q(1))/(M-1)
0014      A0 = A1 / 2.
0015      QN(2) = Q(1) + A0
0016      DO 2 I = 3, M
0017      QN(I) = QN(I-1) + A1
0018      K = NN(I-1) + 1
0019      A2 = QN(I-1) + A0
0020      DO 1 J = K, LXC
0021      IF( Q(J) .LE. A2 ) NN(I) = J
0022      IF( Q(J) .GT. A2 ) GO TO 2
0023      1 CONTINUE
0024      2 CONTINUE
0025      NN(N-1) = LXC
0026      NN(N) = LXT
0027      QN(N-1) = Q(LXT)
0028      WRITE( 6,10 )
0029      10 FORMAT( '0', 9X, 'I', 7X, 'NN(I)', 6X, 'QN(I)' // )
0030      M = N - 1
0031      DO 11 I = 1, M
0032      11 WRITE( 6,12 ) I, NN(I), QN(I)
0033      12 FORMAT( ' ', Z10, 1PE15.3 )
0034      WRITE( 6,12 ) N, NN(N)
0035      WRITE( 6,20 )
0036      RETURN
0037      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**REF**

**DATE = 69338**

**21/51/18**

**TOTAL MEMORY REQUIREMENTS 000478 BYTES**

FORTRAN IV G LEVEL 1, MOD 3

FIRSTV

DATE = 69338

21/51/18

```
0001      SUBROUTINE FIRSTV(LXT1,LXE,LXC,KV)
C
0002      COMMON /BLV/V(341),HR,BETAS,BETAL,BETASL,BETALL
1      /BLQ/Q(341) /BLDD/DOD(341)
0003      DOUBLE PRECISION V,BETAS,BETAL,BETASL,BETALL,HR,Q,A0,
1      A1,A2,ER1,DOD,C1,C2,C3,ER
C
0004      C1 = 2./(1.+HR)
0005      C2 = C1/HR
0006      C3 = 2./HR
0007      KV = 1
0008      OME = 1.5
0009      1 ER = 0.0
0010      EER = 0.0
0011      DO 8 I = 2, LXT1
0012      IF( I .LT. LXE .OR. I .GT. LXC ) GO TO 2
0013      IF( I .EQ. LXE ) GO TO 4
0014      IF( I .EQ. LXC ) GO TO 5
0015      A1 = DEXP(V(I)-Q(I)+BETALL)
0016      GO TO 3
0017      2 A1 = DEXP(V(I)-Q(I)+BETASL)
0018      3 A0 = V(I+1) + V(I-1) - 2.*V(I)
0019      A2 = A1 + 2.
0020      GO TO 7
0021      4 A0 = C1*V(I+1) + C2*V(I-1) - C3*V(I)
0022      A1 = DEXP(V(I)-Q(I)+BETALL)
0023      GO TO 6
0024      5 A0 = C2*V(I+1) + C1*V(I-1) - C3*V(I)
0025      A1 = DEXP(V(I)-Q(I)+BETALL)
0026      6 A2 = A1 + C3
0027      7 A0 = DOD(I) - A1 + A0
0028      A0 = OME*(A0/A2)
0029      V(I) = V(I) + A0
0030      B = DABS(A0/V(I))
0031      IF( B .GT. EER ) EER = B
0032      8 ER = ER + A0**2
C
0033      IF( EER .LT. 0.01 .OR. KV .GE. 100 ) GO TO 10
0034      CALL COME(KV,ER,ER1,OME)
0035      KV = KV + 1
0036      GO TO 1
C
0037      10 WRITE( 6,11 ) KV, OME, EER
0038      11 FORMAT( ' ', 2X, 'KV =',I3,3X,'OME =',F5.2,3X,'EER =',
1      1PE10.2 )
0039      RETURN
0040      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**FIRSTV**

**DATE = 69338**

**21/51/18**

**TOTAL MEMORY REQUIREMENTS 000580 BYTES**

FORTRAN IV G LEVEL 1, MOD 3

COMPQ

DATE = 69338

21/51/18

```
0001      SUBROUTINE  COMPQ(LXT,LXE,LXC,LXT1,N)
C
0002      COMMON /BLQ/Q(341),HS,HL,EN,ALP,DC /BLV/V(341),HR
1      /BLE/E(341) /BLRQ/QN(201,NN(201) /BLAUX/X(341),
2      XX(341),Y(341)
0003      DOUBLE PRECISION Q,HS,HL,HR,EN,DC,V,QN,XX,X,Y,A0,
1      A1,A2,A3,E,ALP,H,HS2,HL2,SUMH
C
0004      HS2 = 2.*HS
0005      HL2 = 2.*HL
0006      SUMH = HL + HS
0007      A1 = HR / SUMH
0008      A2 = 1. / (HR*SUMH)
0009      A3 = (HL-HS) / (HS*HL)
0010      DO 1 I = 1, LXT
0011      IF( I .EQ. 1 ) A0 = (4.*V(I+1)-3.*V(I)-V(I+2))/HS2
0012      IF( I .EQ. LXT ) A0 = (3.*V(I)-4.*V(I-1)+V(I-2))/HS2
0013      IF( I .GT. 1 .AND. I .LT. LXE ) A0=(V(I+1)-V(I-1))/HS2
0014      IF( I.GT.LXC.AND.I.LT.LXT ) A0 = (V(I+1)-V(I-1))/HS2
0015      IF( I.GT.LXE.AND.I.LT.LXC ) A0 = (V(I+1)-V(I-1))/HL2
0016      IF( I .EQ. LXE ) A0 = A1*V(I+1) - A2*V(I-1) + A3*V(I)
0017      IF( I .EQ. LXC ) A0 = A2*V(I+1) - A1*V(I-1) - A3*V(I)
0018      1 E(I) = A0*EN
0019      IF( Q(1) .EQ. Q(LXT) ) GO TO 100
0020      M = N - 1
0021      DO 11 I = 1, LXT
0022      A0 = E(I) / 7.77
0023      IF( A0 .LT. 1.0D-03 ) A1 = 1.0 - A0/2. + A0**2/6.
0024      IF( A0 .GE. 1.0D-03 ) A1 = (1. - DEXP(-A0)) / A0
0025      11 X(I) = -V(I) - DLOG(A1)
C
0026      Y(LXT1) = 0.0
0027      DO 3 I = 1, M
0028      K = N - I
0029      JS = NN(K)
0030      JL = NN(K+1)
0031      DO 2 J = JS, JL
0032      2 XX(J) = X(J) + QN(K)
0033      IF( K .EQ. 1 .OR. K .EQ. M ) H = HS
0034      IF( K .NE. 1 .AND. K .NE. M ) H = HL
0035      CALL EXINT(H,JS,JL,XX,Y,Y(JL),LXT)
0036      IF( K .EQ. 1 ) GO TO 3
0037      IF( Y(JS) .EQ. 0.0 ) A0 = -1000.
0038      IF( Y(JS) .NE. 0.0 ) A0 = DLOG(Y(JS))
0039      Y(JS) = DEXP(QN(K-1)-QN(K)+A0)
0040      3 CONTINUE
C
0041      DO 4 I = 1, LXT1
```

FORTRAN IV G LEVEL 1, MOD 3

COMPO

DATE = 69338

21/51/18

```
0042      AO = Y(I)
0043      IF( AO .EQ. 0.0 ) Y(I) = -1000.
0044      IF( AO .NE. 0.0 ) Y(I) = DLOG(AO)
0045      4 CONTINUE
C
0046      AO = -Q(LXT) + Q(1) - Y(1)
0047      DO 6   I = 2, LXT1
0048      DO 5   J = 1, M
0049      IF( I .GT. NN(J) .AND. I .LE. NN(J+1) ) K = J
0050      5 CONTINUE
0051      Q(I) = DEXP(QN(K)-Q(LXT))
0052      Q(I) = Q(I) - DEXP(AO + Y(I))
0053      Q(I) = Q(I) + DEXP(-Y(1)+Y(I))
0054      6 Q(I) = QN(K) - DLOG(Q(I))
0055      DC = ( DEXP(-Y(1)) - DEXP( AO ) ) * 16. / (9.*ALP)
0056      RETURN
C
0057      100 DC = 0.0
0058      RETURN
0059      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**COMPO**

**DATE = 69338**

**21/51/18**

**TOTAL MEMORY REQUIREMENTS 000A98 BYTES**

FORTRAN IV G LEVEL 1, MOD 3

COMPV

DATE = 69338

21/51/18

```
0001      SUBROUTINE    COMPV(LXT,LXT1,LXE,LXC,RMAX)
0002      C
0003      COMMON /BLV/V(341),HR,BETAS,BETAL,BETASL,BETALL,
0004      1          /BLQ/Q(341) /BLDOD/DOD(341) /BLAUX/X(341),
0005      2          XX(341),Y(341)
0006      DOUBLE PRECISION V,HR,BETAS,BETAL,BETASL,BETALL,Q,DOD
0007      1          ,X,XX,Y,C1,C2,C3,A0,ER,ER1
0008      C
0009      C1 = 2. / (1.+HR)
0010      C2 = C1 / HR
0011      C3 = 2./HR
0012      RMAX = 0.0
0013      DO 6 I = 2, LXT1
0014      IF( I .EQ. LXE ) GO TO 1
0015      IF( I .EQ. LXC ) GO TO 2
0016      AO = V(I+1) + V(I-1) - 2.*V(I)
0017      IF( I .LT. LXE .OR. I .GT. LXC ) GO TO 4
0018      GO TO 3
0019      1 AO = C1*V(I+1) + C2*V(I-1) - C3*V(I)
0020      GO TO 3
0021      2 AO = C2*V(I+1) + C1*V(I-1) - C3*V(I)
0022      3 X(I) = DEXP(V(I)-Q(I)+BETALL)
0023      GO TO 5
0024      4 X(I) = DEXP(V(I)-Q(I)+BETASL)
0025      5 XX(I) = DOD(I) - X(I) + AO
0026      B = DABS(XX(I)) / DOD(I)
0027      IF( B .GT. RMAX ) RMAX = B
0028      6 CONTINUE
0029      C
0030      DO 10 I = 1, LXT
0031      10 Y(I) = 0.0
0032      C
0033      KD = 1
0034      OME = 1.5
0035      20 DMAX = 0.0
0036      ER = 0.0
0037      EER = 0.0
0038      DO 25 I = 2, LXT1
0039      IF( I .EQ. LXE ) GO TO 21
0040      IF( I .EQ. LXC ) GO TO 22
0041      AO = Y(I+1) + Y(I-1)
0042      A1 = 2. + X(I)
0043      GO TO 24
0044      21 AO = C1*Y(I+1) + C2*Y(I-1)
0045      GO TO 23
0046      22 AO = C2*Y(I+1) + C1*Y(I-1)
0047      23 A1 = C3 + X(I)
0048      24 AO = OME*(XX(I)-A1*Y(I)+AO) / A1
```

FORTRAN IV G LEVEL 1, MOD 3

COMPV

DATE = 69338

21/51/18

```
0042      Y(I) = Y(I) + A0
0043      B = DABS(A0)
0044      IF( B .GT. EER ) EER = B
0045      B = DABS(Y(I))
0046      IF( B .GT. DMAX ) DMAX = B
0047      25 ER = ER + A0**2
C
0048      IF( EER/DMAX .LT. 1.0E-02 ) GO TO 30
0049      IF( KD .GE. 100 ) GO TO 30
0050      CALL CCME(KD,ER,ER1,OME)
0051      KD = KD + 1
0052      GO TO 20
C
0053      30 WRITE( 6,40 ) KD,OME,EER,DMAX,RMAX
0054      40 FORMAT( ' ',2X,'KD =',I3,3X,'OME =',F5.2,3X,'EER =',
1          1PE10.2,3X,'DMAX =',1PE10.2,3X,'RMAX =',
2          1PE10.2 )
0055      DO 50 I = 2, LXT1
0056      50 V(I) = V(I) + Y(I)
0057      RETURN
0058      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**COMPV**

**DATE = 69338**

**21/51/18**

**TOTAL MEMORY REQUIREMENTS 000708 BYTES**

FORTRAN IV G LEVEL 1, MOD 3

EXINT

DATE = 69338

21/51/18

```
0001      SUBROUTINE EXINT(H,IS,IF,X,Y,Y0,NDIM)
C
C THIS SUBROUTINE INTEGRATES EXP(X) FROM IS, WHICH IS BETWEEN
C IS AND IF, TO IF AND STORES (RESULT+Y0) AT Y(IF). H IS THE
C MESH SIZE AND NDIM IS THE MAXIMUM DIMENSION OF X AND Y.
C
0002      DOUBLE PRECISION A,H,X,Y,A0,A1,A2,Y0,H2I,HSQ2I,EFCT
0003      DIMENSION X(NDIM), Y(NDIM)
0004      COMMON /BLINT/A1,A2
0005      EXTERNAL EFCT
C
0006      H2I = 1.0 / (2.*H)
0007      HSQ2I = 1.0 / (2.*H**2)
0008      Y(IF) = Y0
0009      LAST = IF - IS
0010      DO 1  II = 2, LAST
0011      I = IF + 1 - II
0012      A0 = X(I)
0013      A1 = (X(I+1)-X(I-1))*H2I
0014      A2 = (X(I+1)+X(I-1)-2.*X(I))*HSQ2I
0015      CALL DQG32(0.0,H,EFCT,A)
0016      1 Y(I) = Y(I+1) + DEXP(A0+DLOG(A))
0017      CALL DQG32(-H,0.0,EFCT,A)
0018      Y(IS) = Y(IS+1) + DEXP(A0+DLOG(A))
0019      RETURN
0020      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**EXINT**

**DATE = 69338**

**21/51/18**

**TOTAL MEMORY REQUIREMENTS 0003A8 BYTES**

FORT	FORTR	FORTRAN IV G LEVEL 1, MOD 3	EFCT	DATE = 69338	21/51/18
000		0001	FUNCTION EFCT(Z)		
000	TOT	0002	C DOUBLE PRECISION A1,A2,Z,EFCT		
000		0003	COMMON /BLINT/A1,A2		
000		0004	EFCT = DEXP(A1*Z + A2*Z**2)		
000		0005	RETURN		
000		0006	END		
000					
000					
000					
000					
001					
001					

FORTRAN IV G LEVEL 1, MOD 3

EFCT

DATE = 69338

21/51/18

```
0001      FUNCTION EFCT(Z)
C
0002      DOUBLE PRECISION A1,A2,Z,EFCT
0003      COMMON /BLINT/A1,A2
0004      EFCT = DEXP(A1*Z + A2*Z**2)
0005      RETURN
0006      END
```

**FORTRAN IV G LEVEL 1, MOD 3**

**EFCT**

**DATE = 69338**

**21/51/18**

**TOTAL MEMORY REQUIREMENTS 000166 BYTES**

FORTRAN IV G LEVEL 1, MOD 3

COME

DATE = 69338

21/51/18

```
0001      SUBROUTINE  COME(KDV,ER,ERP,OME)
C
0002      DOUBLE PRECISION A,ERP,ER
C
0003      IF( KDV .GT. 16 ) GO TO 2
0004      A = DSQRT(ER)
0005      IF( KDV .LE. 15 ) GO TO 1
0006      AA = A/ERP
0007      BB = (AA+OME-1.)/(OME*SQRT(AA))
0008      OME = 2./(1.+SQRT(1.-BB**2))
0009      1 ERP = A
0010      2 RETURN
0011      END
```

FORTRAN IV G LEVEL 1, MOD 3

COME

DATE = 69338

21/51/18

TOTAL MEMORY REQUIREMENTS 00024C BYTES